



# Social shifts in the Late Pre–hispanic US Southwest

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# Agenda

## Introduction

History

Mills et al. (2013): Transformation of social networks in the late pre-Hispanic US Southwest

B-R: Under the magnifying glass

Follow-up questions

## Beyond Brainerd-Robinson

Alternative measures of similarity

Across-Time Comparison

ViSim - A tool to explore similarities among sites





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## History

- ▶ US Southwest (A.D. 1200–1450): large-scale demographic changes
  - ▶ long-distance migration (from north to south in late 1200s)
  - ▶ population aggregation (in south in 1300s)





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Mills et al. (2013): Transformation of social networks in the late pre-Hispanic US Southwest

- ▶ Reconstruct population dynamics using network approach
- ▶ Database: 42 distinct artifacts, 700+ sites/settlements, over 250 years
  - ▶ 515 settlements with  $\geq 30$  artifacts
  - ▶ discretized 250 years into 50-years periods
- ▶ Similarity: Brainerd-Robinson index

$$BR(x, y) = 200 - \sum_{z=1}^p |P_{xz} - P_{yz}|$$

- ▶ Assumption: exchanges movement migrations emulations = Similarity in consumption of wares





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# B-R: Under the magnifying glass

## Sampling bias

▶

	Site A	Site B	Site C
Type 1	80%	80%	0%
Type 2	15%	5%	75%
Type 3	5%	15%	25%

- ▶  $BR(A, B) = 180$     $BR(A, C) = 40$
- ▶  $BR(B, C) = 100$





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## Symmetric similarity

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	Site A	Site B	Site C
Type 1	40%	20%	20%
Type 2	30%	80%	0%
Type 3	30%	0%	80%

▶  $BR(A, B) = 100$   $BR(A, C) = 100$   $BR(B, C) = 40$

▶  $B, C \subset A$





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## Aggregation

	Site A	Site B	Site C	Site D
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<b>Type 2</b>	5%	0%	35%	40%
<b>Type 3</b>	5%	0%	30%	20%
<b>Type 4</b>	10%	0%	10%	5%

- ▶  $BR(A, B) = 160$     $BR(C, D) = 160$
- ▶  $C, D$  both contain all types and differ by at most 10 % in quantity
- ▶  $A, B, B$  contains only Type 1 whereas  $A$  contains all the types.





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## Follow-up questions

1. How do larger and more diverse settlements relate to the smaller and more homogeneous ones?
2. How does population shifts happened within shorter or longer time periods?
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# Reconstructing social shifts

## Proposed Extensions

1. Asymmetric similarity - dominance relationship
2. Ranking of wares/types
3. Index of significance of wares/types
4. Across-time comparison







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## Asymmetric similarity based on dominance relationship

- ▶ Integral: A site  $x$  is dominated by a site  $y$  or the site  $x$  is completely contained in the site  $y$  if and only if the set of distinct items found on site  $x$  is a proper subset of the set of distinct items found on site  $y$ .

$$S_R(x, y) = \begin{cases} 1 & \text{if } B_{x,i} \geq B_{y,i} \forall i \in [1, n] \\ 0 & \text{otherwise} \end{cases}$$

- ▶ Fractional: A site  $x$  is dominated by another site  $y$ , if each type present in  $x$  is also present in  $y$ . It is strictly dominated, if it is dominated and there is at least one type in  $y$  that is not present in  $x$ .

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# Reconstructing social shifts

Similarity based on relative ranking of wares

- ▶ Parametrized: *k*-out-of-top-*l*  
*A pair of sites are similar to each other if they have l of k top ranked wares common among them.*

$$S_R(x, y) = \begin{cases} 1 & \text{if } |V_R^x[1 : k] \cap V_R^y[1 : k]| \geq l \\ 0 & \text{otherwise} \end{cases}$$

- ▶ Non-parametrized: Maximum Quasi-Jaccard  
*A pair of sites are k similar to each other for the maximal k of p types that they can be similar in.*

$$S_R(x, y) = \arg \max_k \frac{|V_R^x[1 : k] \cap V_R^y[1 : k]|}{|V_R^x[1 : k] \cup V_R^y[1 : k]|}$$







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# Reconstructing social shifts

## Index of Significance of Wares

- ▶ *TF – IDF*: (*term frequency–inverse document frequency*), is a numerical statistic that is intended to depict the importance of a word in a document.
  - ▶  $f(i, x)$ : frequency of each ware  $i$  in site  $x$ .
  - ▶  $\frac{|S|}{1 + |\{x \in S : i \in x\}|}$ : inverse the frequency of  $i$  in all sites.
  - ▶  $I(i, x) = f(i, x) \times \frac{|S|}{1 + |\{x \in S : i \in x\}|}$
- ▶ Similarity among sites based on  $I(w_i, x)$
- ▶ Co-occurrence of wares
- ▶ Evolving “identity” of settlements over periods of time.





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# *ViSim*

A tool to explore similarities among settlements

