

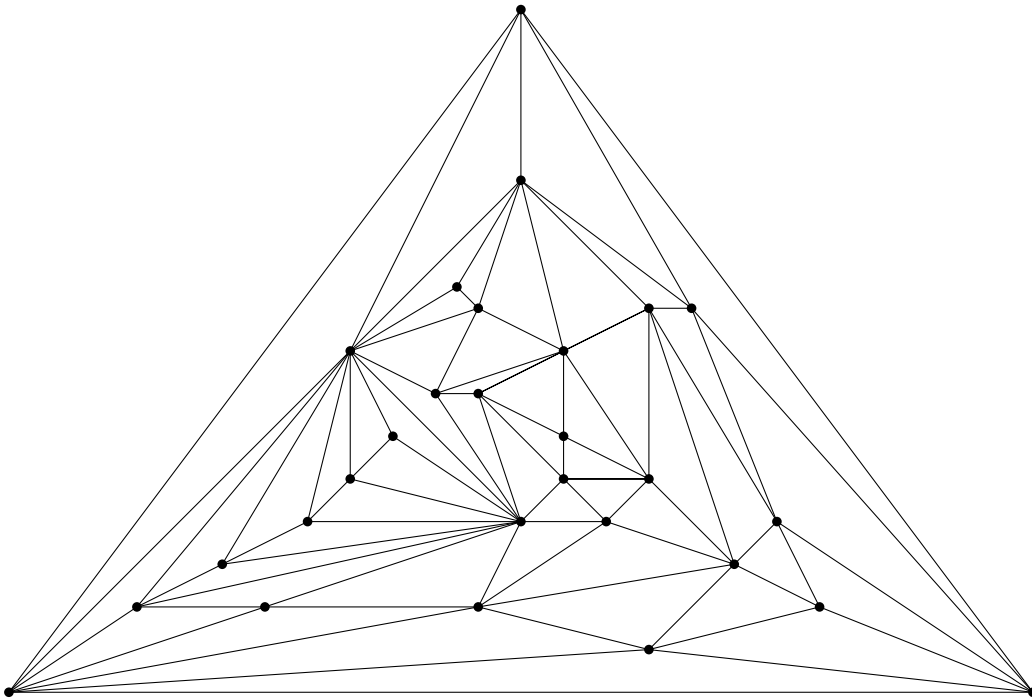
## Assignment 11

**Post Date:** 10 July 2017   **Due Date:** 17 July 2017   **Tutorial:** 19 July 2017

### Problem 1: Separators

**6 Points**

Apply the algorithm from the lecture (see the last slide for a summary) to find a  $\frac{3}{4}$ -balanced cycle separator of size  $\leq 4\sqrt{|V|} + 1$  in the following graph (all faces have the same weight and all nodes and edges have weight 0).



### Problem 2: Balanced Planar Separator

**4 Points**

- Prove or disprove that for every planar graph with  $n \leq 9$ , there exists a  $2/3$ -balanced separator of size  $\leq \sqrt{n}$ .
- Can you find a planar graph with  $n > 9$  vertices that does not have a  $2/3$ -balanced separator of size  $\leq \sqrt{n}$ ? Explain why your example is correct or argue why such an example does not exist.